

Name \_\_\_\_\_

**Test #8**

Non-Calculator Portion (Honor system)

*Show all work for full credit.*

**For problem 1, use the function,**  $f(x) = x^3 + x^2 - 8x - 12.$

**1N. a)** Find the critical number(s).

**d)** Find the x-value for the point(s) of inflection.

**b)** Determine increasing and decreasing intervals of  $f(x)$ .

Inc: \_\_\_\_\_

Dec: \_\_\_\_\_

**e)** Determine intervals of concavity for  $f(x)$ .

Conc. Up: \_\_\_\_\_

Conc. Down: \_\_\_\_\_

**c)** Find all the x-values for relative extrema and classify as maximums or minimums.

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**2N.**  $\lim_{x \rightarrow \infty} \frac{(2x-1)(3-x)}{(x-1)(x+3)}$

(A) -3

(B) -2

(C) 2

(D) 3

(E) nonexistent

3N.

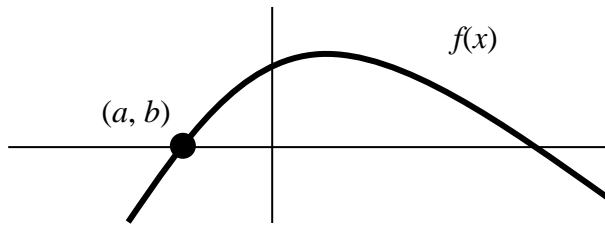
$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2} & \text{if } x \neq 2 \\ 1 & \text{if } x = 2 \end{cases}$$

Let  $f$  be the function defined above. Which of the following statements about  $f$  are true?

- I.  $f$  has a limit at  $x = 2$ .
- II.  $f$  is continuous at  $x = 2$ .
- III.  $f$  is differentiable at  $x = 2$ .

- (A) I only    (B) II only    (C) III only    (D) I and II only    (E) I, II, and III
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4N.



Put in order from least to greatest:  $f(a), f'(a), f''(a)$                        $<$                        $<$

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5N. A function  $f$  is continuous and differentiable on the interval  $[-4, 2]$ , so that  $f$ ,  $f'$ , and  $f''$  have properties as shown in the table below.

$x$	$-4 < x < 0$	$0$	$0 < x < 1$	$1$	$1 < x < 2$
$f(x)$	positive	$0$	negative	$-2$	negative
$f'(x)$	negative	$-1$	negative	$0$	positive
$f''(x)$	negative	$0$	positive	positive	positive

What are the  $x$ -coordinates of the **local maximum** and **local minimum** of  $f$  on the interval  $[-4, 2]$ .

**Show all work for full credit.**

**1C.** Suppose  $x = 8$  is a critical number for a function,  $f$ , with  $f'(x) > 0$  for the interval  $[8, 9]$  and  $f'(x) < 0$  for the interval  $[7, 8]$ . Then  $x = 8$  is:

- (a) a local maximum
- (b) a local minimum
- (c) not a local extremum

**2C.** Given that  $f(x) = -x^2 + 12x - 34$  has a local maximum at  $x = 6$ , choose the correct statement.

- a)  $f'$  is positive on the interval  $(6, \infty)$ .
- b)  $f'$  is positive on the interval  $(-\infty, \infty)$ .
- c)  $f'$  is negative on the interval  $(6, \infty)$ .
- d)  $f'$  is negative on the interval  $(-\infty, 6)$ .
- e) None of these

**3C.** A dog heading due north at a constant speed of 2 meters per second trots past a fire hydrant at  $t = 0$  seconds. Another dog heading due east at a constant speed of 3 meters per second runs by the hydrant at  $t = 1$  second. At  $t = 9$  seconds, the rate of change in the distance between the two dogs is

- a) 3.2 m/sec
- b) 3.6 m/sec
- c) 4.0 m/sec
- d) 4.4 m/sec
- e) 4.8 m/sec

**4C.** The total cost of producing and marketing  $x$  number of units of a certain product is given by

$$C(x) = \frac{4 - 0.02x^2 + .0001x^3}{2}.$$

For what number  $x$  is the total cost a minimum? Round answer to nearest unit.

- A)  $x = 0$
- B)  $x = 100$
- C)  $x = 133$
- D)  $x = 167$

5C. Using calculus, show the work and find the global maximum value and the absolute minimum value of  $g$  on the interval  $[0,4]$ :  $g(x) = \frac{x^2 - 4x + 4}{x + 2}$

6C. Use the Mean Value Theorem to find the values of  $c$ , where  $f'(c)$  is equal to the average rate of change of  $f(x) = x - 2 \sin x$  on the interval  $[0, \pi]$ .

- a)  $c = 0$       b)  $c = 1$       c)  $c = \frac{\pi}{3}$       d)  $c = \frac{\pi}{2}$       e) None of these

7C. A function  $f$  is continuous and differentiable on the interval  $[-4, 2]$ , so that  $f$ ,  $f'$ , and  $f''$  have properties as shown in the table below.

$x$	$-4 < x < 0$	0	$0 < x < 1$	1	$1 < x < 2$
$f(x)$	positive	0	negative	-2	negative
$f'(x)$	negative	-1	negative	0	positive
$f''(x)$	negative	0	positive	positive	positive

What are the  $x$ -coordinates of all **points of inflection** of  $f$  on the interval  $[-4, 2]$ ?