

**Group Work 1, Section 3.8**  
**Four Variations on a Theme**

Consider the following four functions:

$$f(x) = e^{x-1} - 1 \quad g(x) = x^4 - 3x + 2 \quad h(x) = \ln x \quad j(x) = \frac{2}{\pi} \sin\left(\frac{\pi}{2}(x-1)\right)$$

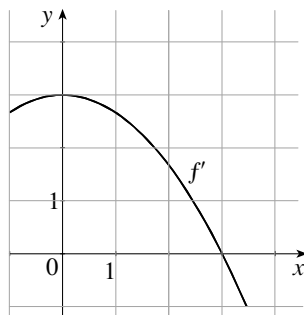
1. Find the linearizations of  $f$ ,  $g$ ,  $h$ , and  $j$  at  $a = 1$ .

2. Compute the values of each of these functions at  $x = 1.1$  and the values of their linearizations. For which function is the approximation best? For which is it worst? Why?

## Group Work 2, Section 3.8

### Linear Approximation

Consider this graph of  $f'(x)$ , the *derivative* of  $f(x)$ .



1. Suppose that  $f(2) = 4$ . Approximate  $f(1.98)$  and  $f(2.02)$  as best you can. Don't just guess. Show your work.
2. Determine whether your approximations were overestimates or underestimates.
3. Suppose you also know that  $f(3) = 7$ . Can you approximate  $f(2.98)$  and  $f(3.02)$ ? Explain your answer.